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Covalency and vibronic couplings make a nonmagnetic $j = 3/2$ ion magneticLei Xu¹, Nikolay A Bogdanov¹, Andrew Princep², Peter Fulde³, Jeroen van den Brink^{1,4} and Liviu Hozoi¹

For $4d^1$ and $5d^1$ spin-orbit-coupled electron configurations, the notion of nonmagnetic $j = 3/2$ quartet ground state discussed in classical textbooks is at odds with the observed variety of magnetic properties. Here we throw fresh light on the electronic structure of $4d^1$ and $5d^1$ ions in molybdenum- and osmium-based double-perovskite systems and reveal different kinds of on-site many-body physics in the two families of compounds: although the sizable magnetic moments and g -factors measured experimentally are due to both metal d -ligand p hybridisation and dynamic Jahn–Teller interactions for $4d$ electrons, it is essentially $d-p$ covalency for the $5d^1$ configuration. These results highlight the subtle interplay of spin-orbit interactions, covalency and electron–lattice couplings as the major factor in deciding the nature of the magnetic ground states of $4d$ and $5d$ quantum materials. Cation charge imbalance in the double-perovskite structure is further shown to allow a fine tuning of the gap between the t_{2g} and e_g levels, an effect of much potential in the context of orbital engineering in oxide electronics.

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INTRODUCTION

A defining feature of d -electron systems is the presence of sizable electron correlations, also referred to as Mott–Hubbard physics. The latter has been traditionally associated with first-series ($3d$) transition-metal (TM) oxides. But recently one more ingredient entered the TM oxide ‘Mottness’ paradigm—large spin-orbit couplings (SOCs) in $4d$ and $5d$ quantum materials.^{1,2} It turns out that for specific t_{2g} -shell electron configurations, a strong SOC can effectively augment the effect of Hubbard correlations:¹ although the $4d$ and $5d$ orbitals are relatively extended objects and the Coulomb repulsive interactions are weakened as compared with the more compact $3d$ states, the spin-orbit-induced level splittings can become large enough to break apart the ‘nonrelativistic’ t_{2g} bands into sets of well-separated, significantly narrower subbands for which even a modest Hubbard U acting on the respective Wannier orbitals can then open up a finite Mott–Hubbard-like gap.¹ On top of that, SOC additionally reshuffles the intersite superexchange.³ The surprisingly large anisotropic magnetic interactions that come into play via the strong SOC in iridates,^{3–8} e.g., are responsible for an exotic assortment of novel magnetic ground states and excitations.^{2,3,9}

For large $t_{2g} - e_g$ splittings, the spin-orbit-coupled t_{2g}^1 and t_{2g}^5 electron configurations can be in first approximation viewed as ‘complementary’: in the simplest picture, the d -shell manifold can be shrunk to the set of $j = 1/2$ and $j = 3/2$ relativistic levels, with a $j = 3/2$ ground state for the TM t_{2g}^1 configuration and a $j = 1/2$ ground state for t_{2g}^5 .^{10–12} Although strongly spin-orbit-coupled t_{2g}^5 oxides and halides—iridates, rhodates and ruthenates, in particular—have generated substantial experimental and theoretical investigations in recent years, much of the properties of $5d$ and $4d$ t_{2g}^1 systems remain to large extent unexplored.

From textbook arguments,^{10–12} the t_{2g}^1 $j = 3/2$ quadruplet should be characterised by a vanishing magnetic moment in cubic

symmetry, due to perfect cancellation of the spin and angular momentum contributions. But this assertion leaves unexplained the wide variety of magnetic properties recently found in $4d^1$ and $5d^1$ cubic oxide compounds.^{13–20} Ba_2YMoO_6 , e.g., develops no magnetic order despite a Curie–Weiss temperature of ≈ -200 K (refs 13,14) and features complex magnetic dynamics that persists down to the mK range, possibly due to either a valence-bond-glass¹⁵ or spin-liquid¹⁶ ground state. Also, $\text{Ba}_2\text{NaOsO}_6$ displays an antiferromagnetic Curie–Weiss temperature^{18,19} but orders ferromagnetically below 7 K (ref. 20), whereas $\text{Ba}_2\text{LiOsO}_6$ is a spin-flop antiferromagnet.²⁰

Here we carry out a detailed *ab initio* investigation of the Mo^{5+} $4d^1$ and Os^{7+} $5d^1$ relativistic electronic structure in the double-perovskite compounds Ba_2YMoO_6 , $\text{Ba}_2\text{LiOsO}_6$ and $\text{Ba}_2\text{NaOsO}_6$. In addition to providing reliable results for the energy scale of the d -level splittings, $t_{2g} - e_g$ and induced by SOC within the t_{2g}^1 manifold, we analyse the role of TM $d-O p$ orbital mixing plus the strength of electron–lattice couplings. It is found that strong metal $d-O p$ hybridisation generates a finite magnetic moment even for perfectly cubic environment around the TM site, providing *ab initio* support to the phenomenological covalency factor introduced in this context by Stevens.²¹ The TM d^1 magnetic moment is further enhanced by tetragonal distortions, against which the octahedral oxygen cage is unstable. According to our results, such Jahn–Teller (JT) effects are particularly strong for the Mo $4d^1$ ions in Ba_2YMoO_6 . Although additional investigations are needed for clarifying the role of intersite cooperative couplings,^{22,23} our calculations emphasise the high sensitivity of the effective magnetic moments to both metal–ligand covalency effects and local JT physics. The material dependence for the ratio among the strengths of the spin-orbit interaction, the JT coupling parameter and the effective covalency factor that we compute

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here provide a solid basis for future studies addressing the role of intersite interactions on the double-perovskite fcc lattice.

RESULTS

Quantum chemistry calculations were first performed to resolve the essential features of the electronic structure of the cubic lattice configuration, without accounting for electron–lattice couplings (see Materials and methods for computational details and Figure 1 for a sketch of a three-dimensional double-perovskite crystal). Results for the splitting between the $\text{Mo}^{5+} t_{2g}^1$ $j=3/2$ and $j=1/2$ spin–orbit states, $\Delta_{3/2 \rightarrow 1/2}$, are provided in Table 1 at two levels of approximation, i.e., multiconfiguration complete-active-space self-consistent field (CASSCF) and multireference configuration interaction (MRCI) with single and double excitations on top of the CASSCF wave function.²⁴ Knowing the splitting $\Delta_{3/2 \rightarrow 1/2}$, the strength of the SOC parameter can be easily derived as $\lambda = \frac{2}{3} \Delta_{3/2 \rightarrow 1/2}^{\text{CASSCF}}$.¹¹ The resulting λ of 89 meV is somewhat smaller than earlier estimates of 99 meV for Mo^{5+} impurities in SrTiO_3 .²⁵ A most interesting finding, however, is that despite the cubic environment the quantum chemistry calculations yield a

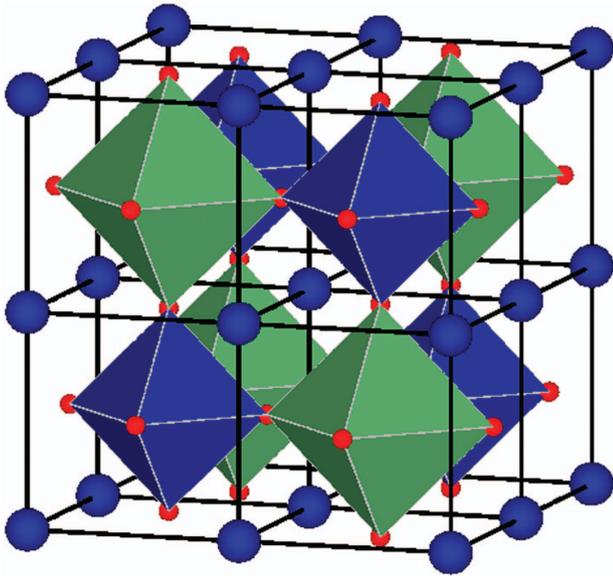


Figure 1. Sketch of the atomic positions in a cubic double-perovskite compound, $\text{Ba}_2\text{BB}'\text{O}_6$. B stands here for Y , Na or Li (site at the centre of a dark-blue octahedron); B' is either Mo or Os (site at the centre of a light-green octahedron). O ions are shown as small red spheres, whereas the Ba sites are the larger blue spheres.

$4d^1$ electronic structure	CASSCF	MRCI
$\Delta_{3/2 \rightarrow 1/2}$ (eV)	0.133	0.130
$\Delta_{t_{2g} \rightarrow e_g}$ (eV)	4.80	4.51
g_{\parallel}	0.18	0.20

Abbreviations: CASSCF, complete-active-space self-consistent field; MRCI, multireference configuration interaction; SOC, spin–orbit coupling. Three orbitals ($4d t_{2g}$) were active in the CASSCF calculation for $\Delta_{3/2 \rightarrow 1/2}$, whereas five orbitals were active in the calculations for g_{\parallel} and $\Delta_{t_{2g} \rightarrow e_g}$ (sans SOC for the latter).

nonvanishing magnetic moment and a finite g -factor. This obviously does not fit the nonmagnetic $j=3/2$ quartet ground state assumed to arise in standard textbooks on crystal-field theory^{11,12} from exact cancellation between the spin and the orbital moments.

At a qualitative level, it has been argued by Stevens²¹ that finite g -factor values can in fact occur for $j=3/2$ ions due to TM–O covalency on the TM O_6 octahedron. For better insight into the nature of such effects, we therefore performed a simple numerical experiment in which the six ligands coordinating the reference $\text{Mo}^{5+} 4d^1$ ion are replaced by -2 point charges with no atomic basis functions. In that additional set of computations the magnetic moment and the g -factor do vanish, in agreement with the purely ionic picture of Kotani, Abragam and Bleaney.^{10,11} This shows that one tuning knob for switching magnetism on is indeed the TM $4d - \text{O} 2p$ orbital hybridisation. The latter is strong for high ionisation states such as Mo^{5+} (as the tails of the $4d$ -like valence orbitals indicate in the case the nearest-neighbor ligands are provided with atomic basis sets, see Figure 2a), gives rise to partial quenching of the orbital moment and makes that the exact cancellation between the spin and the orbital moments no longer holds.

We find that this effect is even stronger for the formally $7+ \text{Os}$ ion in $\text{Ba}_2\text{LiOsO}_6$ and $\text{Ba}_2\text{NaOsO}_6$. As shown in Table 2, g -factors as large as 0.4 are computed in this case. The quantum chemistry results also allow us to estimate the strength of the effective $\text{Os}^{7+} 5d^1$ SOC constant, with $\lambda = \frac{2}{3} \Delta_{3/2 \rightarrow 1/2}^{\text{CASSCF}} = 387$ meV, lower than $\lambda = 468$ meV in tetravalent $5d^5$ iridates.²⁶

As the t_{2g}^1 electron configuration is susceptible to JT effects, we carried out further investigations on the stability of an ideal TM O_6 octahedron against tetragonal (z axis) distortions. A total-energy profile for specified geometric configurations is provided in Figure 2c for an embedded MoO_6 octahedron. It is seen that the minimum corresponds to $\sim 3\%$ tetragonal compression, as compared with the cubic octahedron of the $Fm\bar{3}m$ crystalline structure.¹⁴ As expected, the magnetic moment rapidly increases in the presence of distortions, as illustrated in Table 3 and Figure 2d.

Depending on further details related to the strength of the intersite couplings among ‘JT centres’, static deformations away from cubic symmetry may be realised in some systems, as observed for example in the $\text{Re}^{6+} 5d^1$ double-perovskite $\text{Sr}_2\text{MgReO}_6$ (ref. 27) and rare-earth molybdates.^{28,29} If the local JT couplings and intersite interactions are relatively weak, one may be left on the other hand in a dynamic JT regime, as earlier pointed out for the particular t_{2g}^1 configuration by, e.g., Kahn and Kettle.³⁰ The relevant vibrational modes that couple to the ${}^2T_{2g}(t_{2g}^1)$ electronic term are those of E_g symmetry ($(3z^2 - r^2)$ - and $(x^2 - y^2)$ -like). From the quantum chemistry calculations, we find that the potential-energy well is significantly shallower for these normal coordinates, as compared with z axis-only compression. The value we computed for the Mo^{5+} ion in Ba_2YMoO_6 , ≈ 40 meV, is comparable to the estimate made in the 1970s for $\text{Mo}^{5+} t_{2g}^1$ impurity ions within the SrTiO_3 matrix, ≈ 60 meV.²⁵ For the osmates, the depth of this potential well is much reduced, with E_{JT} values in the range of 10–15 meV by spin–orbit MRCI calculations (Table 4).

The vibronic model of Kahn and Kettle³⁰ provides specific expressions for the g -factors. In particular, g_{\parallel} can be parametrised as³⁰

$$g_{\parallel} = 2(1 - k_{\text{cov}}k_{\text{vib}}), \quad (1)$$

where k_{cov} is Stevens’ covalency factor²¹ and

$$k_{\text{vib}} = \exp[-x/(1 + \rho)]. \quad (2)$$

The parameters x and ρ are defined as³⁰ $x = 3E_{\text{JT}}/2\hbar\omega$ and $\rho = 3\lambda/2\hbar\omega$, where $\hbar\omega$ is the E_g -mode vibrational energy and $g_{\perp} = 0$ by symmetry.^{11,21,30} Recent infrared transmission spectra

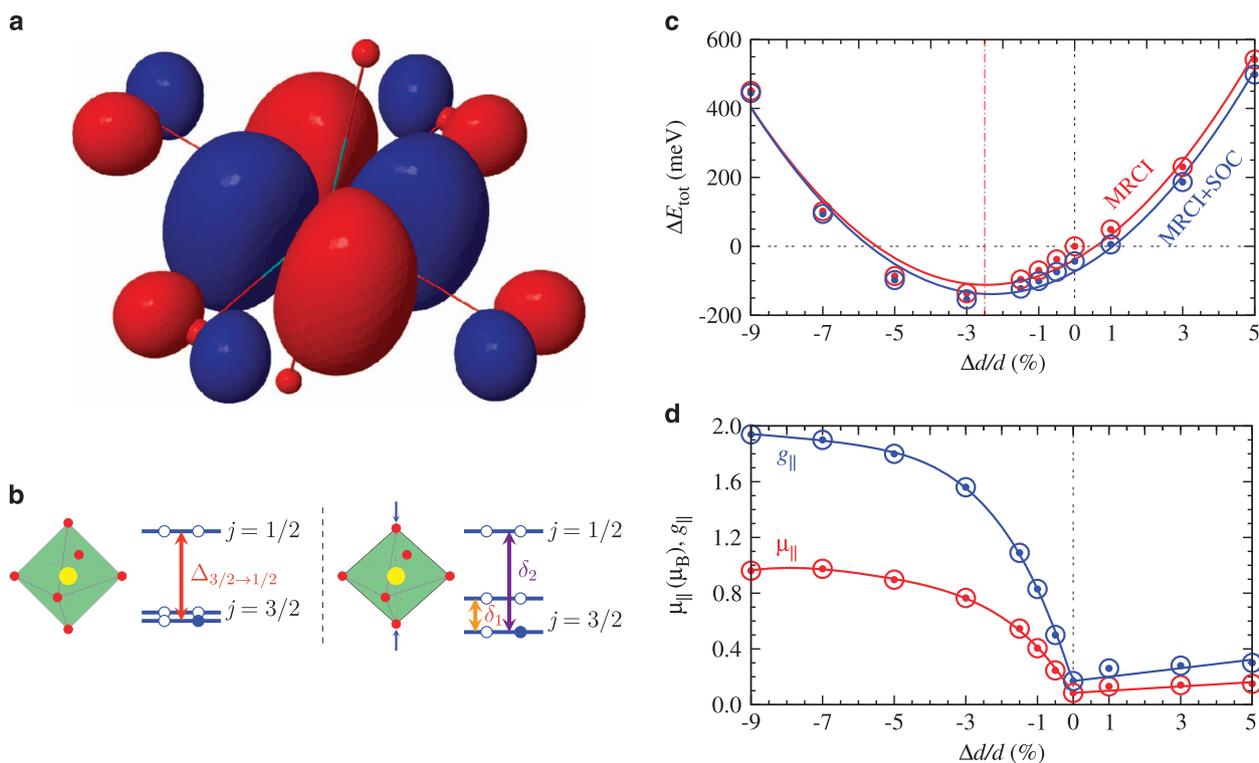


Figure 2. (a) Mo $4d$ t_{2g} charge distribution as obtained by CASSCF calculations. The tails at the nearest-neighbor O sites have substantial weight. (b) TM t_{2g} splittings in cubic (left) and tetragonal (right) symmetry; $\delta_1 = 0$ and $\delta_2 = \Delta_{3/2 \rightarrow 1/2}$ for cubic octahedra. (c) Ground-state energy as function of z axis tetragonal distortion, MRCI results both with and without spin-orbit coupling. (d) Variation of the Mo $4d^1$ magnetic moment ($\mu_{||}$) and g -factor ($g_{||}$) with the amount of z axis tetragonal distortion, MRCI results including spin-orbit interactions.

Table 2. Os^{7+} $5d$ -shell splittings ($j = 3/2$ to $j = 1/2$ and $t_{2g} - e_g$) and 'static' $g_{||}$ factors in cubic $\text{Ba}_2\text{LiOsO}_6$ and $\text{Ba}_2\text{NaOsO}_6$

$5d^1$ electronic structure	CASSCF	MRCI
$\text{Ba}_2\text{LiOsO}_6$		
$\Delta_{3/2 \rightarrow 1/2}$	0.58	0.56
$\Delta_{t_{2g} \rightarrow e_g}$	6.17 (6.44)	5.95 (6.21)
$g_{ }$	0.39	0.40
$\text{Ba}_2\text{NaOsO}_6$		
$\Delta_{3/2 \rightarrow 1/2}$	0.58	0.57
$\Delta_{t_{2g} \rightarrow e_g}$	6.41 (6.68)	6.19 (6.45)
$g_{ }$	0.31	0.40

Abbreviations: CASSCF, complete-active-space self-consistent field; MRCI, multireference configuration interaction; SOC, spin-orbit coupling. Only the $5d$ t_{2g} orbitals were active in the CASSCF calculation for $\Delta_{3/2 \rightarrow 1/2}$; all five $5d$ orbitals were active in the calculations for $g_{||}$ and $\Delta_{t_{2g} \rightarrow e_g}$. For the latter, values including SOC are provided within parantheses. All energies in eV.

Table 3. Mo^{5+} t_{2g}^1 electronic structure with 'static' tetragonal squeezing of the reference MoO_6 octahedron

MoO_6 flattening	0.5%	1.5%	3%	5%
$\Delta_{t_{2g}}$	0.02	0.07	0.15	0.27
δ_1	0.02	0.05	0.12	0.24
δ_2	0.14	0.17	0.23	0.33
$\mu_{ }$ (μ_B)	0.24	0.55	0.75	0.89
$g_{ }$ ($k_{\text{vib}} = 1$)	0.50	1.09	1.55	1.80

Abbreviations: CASSCF, complete-active-space self-consistent field; MRCI, multireference configuration interaction; SOC, spin-orbit coupling. Only the t_{2g}^1 configuration was considered in the reference CASSCF. $\Delta_{t_{2g}}$ is t_{2g} tetragonal splitting without SOC, δ_1 and δ_2 are excitation energies within the t_{2g}^1 manifold with SOC accounted for ($\delta_1 = 0$ and $\delta_2 = \Delta_{3/2 \rightarrow 1/2}$ for cubic octahedra, see Figure 2b). MRCI results, all energies in eV.

Table 4. TM $g_{||}$ factors using the Kahn-Kettle vibronic model³⁰ and *ab initio* estimates for λ , k_{cov} and E_{JT}

	E_{JT}	x	ρ	k_{vib}	k_{cov}	$g_{ }$
$\text{Mo}^{5+} 4d^1$, Ba_2YMoO_6	40	0.86	1.90	0.74	0.90	0.66
$\text{Os}^{7+} 5d^1$, $\text{Ba}_2\text{LiOsO}_6$	10	0.21	8.29	0.98	0.80	0.44
$\text{Os}^{7+} 5d^1$, $\text{Ba}_2\text{NaOsO}_6$	15	0.32	8.29	0.97	0.80	0.45

$x = 3E_{\text{JT}}/2\hbar\omega$, $\rho = 3\lambda/2\hbar\omega$, $\hbar\omega$ is set to 70 meV (refs 17,31) and $g_{||} = 2(1 - k_{\text{cov}}k_{\text{vib}})$.

indicate that $\hbar\omega \approx 560 \text{ cm}^{-1} \approx 70 \text{ meV}$ for the bond-stretching phonons.^{17,31} The effective parameter k_{cov} we can easily evaluate from the static $g_{||}$ values obtained in the MRCI spin-orbit treatment (Tables 1 and 2) if vibronic interactions are neglected ($k_{\text{vib}} = 1$ for 'frozen' cubic octahedra), with $k_{\text{cov}} \equiv 1 - g_{||}^{\text{MRCI}}/2$. This yields covalency reduction factors of 0.90 for Ba_2YMoO_6 and 0.80 for the osmates.

Estimates for g_{\parallel} are provided in Table 4, using the Kahn–Kettle vibronic model and the quantum chemistry results for λ , k_{cov} and E_{JT} . It is seen that a large ρ/x ratio (i.e., large λ/E_{JT}) makes that g_{\parallel} is generated mostly through covalency effects in the osmates, with minor contributions from vibronic couplings. On the other hand, the small ρ/x ratio in Ba_2YMoO_6 gives rise to a strong enhancement of g_{\parallel} through vibronic effects, with a factor of nearly 4 between $(1 - k_{\text{cov}}k_{\text{vib}})$ and $(1 - k_{\text{cov}})$. This way, the interesting situation arises that the TM magnetic moment is mainly due to vibronic effects in Ba_2YMoO_6 and predominantly to strong covalency in $\text{Ba}_2\text{LiOsO}_6$ and $\text{Ba}_2\text{NaOsO}_6$.

DISCUSSION

Experimentally, the measured magnetic moments are indeed significantly smaller in $\text{Ba}_2\text{LiOsO}_6$ and $\text{Ba}_2\text{NaOsO}_6$ (refs 19,20) as compared with Ba_2YMoO_6 (refs 13,14,17,25). With regard to the estimates we make here for g_{\parallel} , possible sources of errors concern the accuracy of the calculated E_{JT} when using the experimental crystal structure as reference and correlation and polarisation effects beyond a single TM O_6 octahedron.^{32,33} The latter effects would only increase E_{JT} . With respect to the former aspect, it is known that by advanced quantum chemistry calculations, the lattice constants of TM oxides can be computed with deviations of $< 0.5\%$ from the measured values,³² which implies rather small corrections to E_{JT} . Interestingly, recent findings of additional phonon modes at low temperatures¹⁷ indicate static distortions of the MoO_6 octahedra in Ba_2YMoO_6 and indeed a rather large E_{JT} . More detailed investigations on this matter are left for future work. Valuable experimental data that can be directly compared with our calculations would be the results of electron spin resonance measurements of the g -factors.

It is also worth pointing out that using the Kahn–Kettle model even a E_{JT} of 75 meV, five to seven times larger than the values computed by MRCI for the osmates (Table 4), still yields a rather moderate g_{\parallel} factor of 0.65 for the Os $5d^1$ ion. Such g_{\parallel} factors of 0.4–0.6 compare quite well with the low-temperature magnetic moment derived from magnetisation and muon spin relaxation measurements on $\text{Ba}_2\text{NaOsO}_6$, $\approx 0.2 \mu_{\text{B}}$.^{19,20} For the Mo $4d^1$ ion in Ba_2YMoO_6 , the computed g_{\parallel} factor is much more sensitive to variations of E_{JT} —increasing E_{JT} from, e.g., 40–200 meV enhances g_{\parallel} of Equation (1) from ≈ 0.6 to ≈ 1.6 .

One other remarkable prediction of Kahn and Kettle³⁰ is that the splitting of the $j=3/2$ and $j=1/2$ states is increased through vibronic couplings, by a factor

$$\gamma = 1 + x \frac{3 + \rho}{3(\rho^2 - 1)}. \quad (3)$$

This effect turns out to be small in the osmates, given the small x and large ρ in those compounds. But we compute a strong modification of the $j=3/2$ to $j=1/2$ excitation energy for Ba_2YMoO_6 , from ~ 0.13 eV in the absence of vibronic interactions (Table 1) to ≈ 0.20 eV with JT effects included ($E_{\text{JT}} = 40$ meV). Experimentally, the situation can be clarified by direct resonant inelastic X-ray scattering (RIXS) measurements on Ba_2YMoO_6 . High-resolution RIXS measurements could also address the occurrence of static distortions at low temperatures, suggested for Ba_2YMoO_6 on the basis of extra phonon modes in the low- T infrared transmission spectra¹⁷ and for $\text{Ba}_2\text{NaOsO}_6$ from the integrated entropy through the magnetic phase transition at ~ 7 K.¹⁹ According to the MRCI data in Table 3, a reduction by 0.5–1.5% of the interatomic distances on one set of O–Mo–O links already gives a splitting of 20–50 meV of the low-lying spin–orbit states. Splittings of this size should be accessible with last-generation RIXS apparatus.

Also of interest is an experimental confirmation of the unusually large $t_{2g} - e_g$ gap we predict in the double-perovskite heptavalent osmates, ≥ 6 eV (Table 2). According to the results of additional

computations we carried out, the source of this exceptional d -level splitting is the stabilisation of the Os t_{2g} states due to the large effective charge (formally 7+) at the nearest-neighbor Os sites. The latter are situated on the axes along which the lobes of the t_{2g} orbitals are oriented; in contrast, the lobes of the e_g functions point towards the monovalent species (Li^{1+} or Na^{1+}). For example, test CASSCF calculations in which the size of the point charges placed at the 12 Os and 6 alkaline-ion nearest-neighbor sites are modified from the formal ionic values 7+ and 1+ ($12 \times 7 + 6 \times 1 = 90$) to 5+ and 5+ ($12 \times 5 + 6 \times 5 = 90$) show a reduction of about 2 eV of the $t_{2g} - e_g$ level splitting. Similar effects, with relative shifts and even inversion of the d -electron energy levels due to charge imbalance at nearby cation sites, were recently evidenced in Sr_2RhO_4 and Sr_2IrO_4 ,^{8,26} the rare-earth 227 iridates $R_2\text{Ir}_2\text{O}_7$ (ref. 34) and $\text{Cd}_2\text{Os}_2\text{O}_7$.³⁵ The mechanism has not been thoroughly explored so far experimentally but seems to hold much potential in the context of orbital engineering in TM compounds.

To summarise, it is well known that nominal orbital degeneracy gives rise in $3d$ TM oxides to subtle couplings between the electronic and lattice degrees of freedom and very rich physics. Here we resolve the effect of electron–lattice interactions on the magnetic properties of heavier, $4d$ and $5d$ TM ions with a formally degenerate t_{2g} electron configuration in the double-perovskite materials Ba_2YMoO_6 , $\text{Ba}_2\text{LiOsO}_6$ and $\text{Ba}_2\text{NaOsO}_6$. In particular, using advanced quantum chemistry electronic-structure calculations, we reconcile the notion of a nonmagnetic spin–orbit-coupled $t_{2g}^1 j=3/2$ ground state put forward by Kotani, Abragam, Bleaney and others^{10–12} with the variety of magnetic properties recently observed in $4d^1$ and $5d^1$ double perovskites. Our analysis shows that the sizable magnetic moments and g -factors found experimentally are due to strong TM d -ligand p hybridisation and dynamic JT effects, providing new perspectives on the interplay between metal–ligand interactions and SOCs in TM oxides. It also highlights the proper theoretical frame for addressing the remarkably rich magnetic properties of d^1 double perovskites^{2,15,16,19,20} in particular. Over the past two decades, vibronic couplings have unjustifiably received low attention in the case of these intriguing materials.

MATERIALS AND METHODS

All *ab initio* calculations were carried out with the quantum chemistry package Molpro.³⁶ Crystallographic data as derived in ref. 14 for Ba_2YMoO_6 and in ref. 18 for $\text{Ba}_2\text{LiOsO}_6$ and $\text{Ba}_2\text{NaOsO}_6$ were employed.

We used effective core potentials, valence basis functions of triple-zeta quality and two f polarisation functions for the reference Mo/Os ions^{37,38} for which the d -shell excitations are explicitly computed. All-electron triple-zeta basis sets supplemented with two d polarisation functions³⁹ were applied for each of the six adjacent O ligands. The eight Ba nearest neighbours were in each case modelled by Ba^{2+} ‘total-ion’ pseudopotentials supplemented with a single s function.⁴⁰ For Ba_2YMoO_6 , the six nearby Y sites were described by effective core potentials and valence basis functions of double-zeta quality.³⁷ In $\text{Ba}_2\text{LiOsO}_6$ and $\text{Ba}_2\text{NaOsO}_6$, we employed total-ion pseudopotentials for the six nearest Li and Na cations and sets of one s and one p functions.⁴¹ The farther solid-state surroundings enter the quantum chemistry calculations at the level of a Madelung ionic potential. How the complexity and accuracy of quantum chemistry calculations for an infinite solid can be systematically increased is addressed in, e.g., refs 32,33,42,43.

For the CASSCF calculations of the d -shell splittings, we used active spaces of either three (t_{2g}) or five (t_{2g} plus e_g) orbitals. The CASSCF optimisations were carried out for an average of either the ${}^2T_{2g}(t_{2g}^1)$ or ${}^2T_{2g}(t_{2g}^1) + {}^2E_{2g}(e_g^1)$ eigenfunctions of the scalar relativistic Hamiltonian. All O $2p$ and Mo/Os $4d/5d$ electrons on the reference TM O_6 octahedron were correlated in the MRCI treatment. The latter was performed with single and double substitutions with respect to the CASSCF reference, as described in refs 44,45. The spin–orbit treatment was carried out according to the procedure described in ref. 46.

The g -factors were computed following a scheme proposed by Bolvin⁴⁷ and Vancoillie.⁴⁸ For a Kramers-doublet ground state $\{\psi, \bar{\psi}\}$, the Abragam–Bleaney tensor¹¹ $G = gg^T$ can be expressed in matrix form as

$$G_{kl} = 2 \sum_{u,v=\psi,\bar{\psi}} \langle u | \hat{L}_k + g_e \hat{S}_k | v \rangle \langle v | \hat{L}_l + g_e \hat{S}_l | u \rangle \\ = \sum_{m=x,y,z} \left(\Lambda_{km} + g_e \sum_{km} \right) \left(\Lambda_{lm} + g_e \sum_{lm} \right), \quad (4)$$

where g_e is the free-electron g -factor and

$$\Lambda_{kx} = 2\text{Re}[\langle \bar{\psi} | \hat{L}_k | \psi \rangle], \quad \sum_{kx} = 2\text{Re}[\langle \bar{\psi} | \hat{S}_k | \psi \rangle], \\ \Lambda_{ky} = 2\text{Im}[\langle \bar{\psi} | \hat{L}_k | \psi \rangle], \quad \sum_{ky} = 2\text{Im}[\langle \bar{\psi} | \hat{S}_k | \psi \rangle], \\ \Lambda_{kz} = 2[\langle \psi | \hat{L}_k | \psi \rangle], \quad \sum_{kz} = 2[\langle \psi | \hat{S}_k | \psi \rangle]. \quad (5)$$

The matrix elements of \hat{L} were extracted from the Molpro outputs, whereas the matrix elements of \hat{S} were derived using the conventional expressions for the generalised Pauli matrices:

$$(\hat{S}_z)_{MM'} = M\delta_{MM'}, \\ (\hat{S}_x)_{MM'} = \frac{1}{2}\sqrt{(S+M)(S-M+1)}\delta_{M-1,M'} \\ + \frac{1}{2}\sqrt{(S-M)(S+M+1)}\delta_{M+1,M'}, \\ (\hat{S}_y)_{MM'} = -\frac{i}{2}\sqrt{(S+M)(S-M+1)}\delta_{M-1,M'} \\ + \frac{i}{2}\sqrt{(S-M)(S+M+1)}\delta_{M+1,M'}. \quad (6)$$

The g -factors were calculated as the positive square roots of the three eigenvalues of G .

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CONTRIBUTIONS

L.X. carried out the *ab initio* quantum chemistry calculations, with assistance from N. A.B., A.P., P.F. and L.H. The mapping of the *ab initio* data onto the effective vibronic model was performed by L.X., L.H. and P.F. L.H., P.F. and J.vdB. designed the project. L. X. and L.H. wrote the paper, with contributions from all other coauthors.

COMPETING INTERESTS

The authors declare no conflict of interest.

REFERENCES

- Kim, B. J. *et al.* Novel $J_{\text{eff}}=1/2$ Mott state induced by relativistic spin-orbit coupling in Sr_2IrO_4 . *Phys. Rev. Lett.* **101**, 076402 (2008).
- Witczak-Krempa, W., Chen, G., Kim, Y. B. & Balents, L. Correlated quantum phenomena in the strong spin-orbit regime. *Annu. Rev. Condens. Matter Phys.* **5**, 57–82 (2014).
- Jackeli, G. & Khaliullin, G. Mott insulators in the strong spin-orbit coupling limit: from Heisenberg to a quantum compass and Kitaev models. *Phys. Rev. Lett.* **102**, 017205 (2009).
- Gretarsson, H. *et al.* Magnetic excitation spectrum of Na_2IrO_3 probed with resonant inelastic x-ray scattering. *Phys. Rev. B* **87**, 220407 (2013).
- Chun, S. H. *et al.* Direct evidence for dominant bond-directional interactions in a honeycomb lattice iridate Na_2IrO_3 . *Nat. Phys.* **11**, 462–466 (2015).
- Yamaji, Y., Nomura, Y., Kurita, M., Arita, R. & Imada, M. First-principles study of the honeycomb-lattice iridates Na_2IrO_3 in the presence of strong spin-orbit interaction and electron correlations. *Phys. Rev. Lett.* **113**, 107201 (2014).
- Katukuri, V. M. *et al.* Kitaev interactions between $j=1/2$ moments in honeycomb Na_2IrO_3 are large and ferromagnetic: insights from *ab initio* quantum chemistry calculations. *New J. Phys.* **16**, 013056 (2014).
- Bogdanov, N. A. *et al.* Orbital reconstruction in nonpolar tetravalent transition-metal oxide layers. *Nat. Commun.* **6**, 7306 (2015).

- Chaloupka, J., Jackeli, G. & Khaliullin, G. Kitaev-Heisenberg model on a honeycomb lattice: Possible exotic phases in iridium oxides A_2IrO_3 . *Phys. Rev. Lett.* **105**, 027204 (2010).
- Kotani, M. On the magnetic moment of complex ions (I). *J. Phys. Soc. Jpn* **4**, 293–297 (1949).
- Abragam, A. & Bleaney, B. *Electron Paramagnetic Resonance of Transition Ions*, 417–426 (Clarendon Press, 1970).
- Mabbs, F. E. & Machin, D. J. *Magnetism and Transition Metal Complexes*, 68–84 (Chapman and Hall, 1973).
- Cussen, E. J., Lynham, D. R. & Rogers, J. Magnetic order arising from structural distortion: Structure and magnetic properties of $\text{Ba}_2\text{LnMoO}_6$. *Chem. Mater.* **18**, 2855–2866 (2006).
- Aharen, T. *et al.* Magnetic properties of the geometrically frustrated $S=1/2$ antiferromagnets $\text{La}_2\text{LiMoO}_6$ and Ba_2YMoO_6 , with the B-site ordered double perovskite structure: Evidence for a collective spin-singlet ground state. *Phys. Rev. B* **81**, 224409 (2010).
- A de Vries, M., McLaughlin, A. C. & Bos, J.-W. G. Valence bond glass on an fcc lattice in the double perovskite Ba_2YMoO_6 . *Phys. Rev. Lett.* **104**, 177202 (2010).
- Carlo, J. P. *et al.* Triplet and in-gap magnetic states in the ground state of the quantum frustrated fcc antiferromagnet Ba_2YMoO_6 . *Phys. Rev. B* **84**, 100404 (2011).
- Qu, Z. *et al.* Spin-phonon coupling probed by infrared transmission spectroscopy in the double perovskite Ba_2YMoO_6 . *J. Appl. Phys.* **113**, 17E137 (2013).
- Stitzer, K. E., Smith, M. D. & zur Loye, H.-C. Crystal growth of Ba_2MOsO_6 ($M = \text{Li, Na}$) from reactive hydroxide fluxes. *Solid State Sci.* **4**, 311–316 (2002).
- Erickson, A. S. *et al.* Ferromagnetism in the Mott insulator $\text{Ba}_2\text{NaOsO}_6$. *Phys. Rev. Lett.* **99**, 016404 (2007).
- Steele, A. J. *et al.* Low-moment magnetism in the double perovskites Ba_2MOsO_6 ($M = \text{Li, Na}$). *Phys. Rev. B* **84**, 144416 (2011).
- Stevens, K. W. H. On the magnetic properties of covalent XY_6 complexes. *Proc. R. Soc. Lond. A Math. Phys. Sci.* **219**, 542–555 (1953).
- Chen, G., Pereira, R. & Balents, L. Exotic phases induced by strong spin-orbit coupling in ordered double perovskites. *Phys. Rev. B* **82**, 174440 (2010).
- Gangopadhyay, S. & Pickett, W. E. Spin-orbit coupling, strong correlation, and insulator-metal transitions: The $J_{\text{eff}}=3/2$ ferromagnetic Dirac-Mott insulator $\text{Ba}_2\text{NaOsO}_6$. *Phys. Rev. B* **91**, 045133 (2015).
- Helgaker, T., Jørgensen, P. & Olsen, J. *Molecular Electronic-Structure Theory* (Wiley, 2000).
- Faughnan, B. W. Electron-paramagnetic-resonance spectrum of Mo^{5+} in SrTiO_3 —an example of the dynamic Jahn-Teller effect. *Phys. Rev. B* **5**, 4925–4931 (1972).
- Katukuri, V. M. *et al.* Electronic structure of low-dimensional $4d^2$ oxides: Interplay of ligand distortions, overall lattice anisotropy, and spin-orbit interactions. *Inorg. Chem.* **53**, 4833–4839 (2014).
- Wiebe, C. R. *et al.* Frustration-driven spin freezing in the $S=1/2$ fcc perovskite $\text{Sr}_2\text{MgReO}_6$. *Phys. Rev. B* **68**, 134410 (2003).
- McLaughlin, A. C. Simultaneous Jahn-Teller distortion and magnetic order in the double perovskite $\text{Ba}_2\text{SmMoO}_6$. *Phys. Rev. B* **78**, 132404 (2008).
- Wallace, T. K., Colman, R. H. & McLaughlin, A. C. A variable temperature synchrotron X-ray diffraction study of the ferroelastic double perovskite $\text{Ba}_2\text{GdMoO}_6$. *Phys. Chem. Chem. Phys.* **15**, 8672–8677 (2013).
- Kahn, O. & Kettle, S. F. A. Vibronic coupling in cubic complexes. *Mol. Phys.* **29**, 61–79 (1975).
- Prosandeev, S. A., Waghmare, U., Levin, I. & Maslar, J. First-order Raman spectra of $\text{AB}_{1/2}\text{B}''_{1/2}\text{O}_3$ double perovskites. *Phys. Rev. B* **71**, 214307 (2005).
- Doll, K., Dolg, M., Fulde, P. & Stoll, H. Quantum chemical approach to cohesive properties of NiO . *Phys. Rev. B* **55**, 10282–10288 (1997).
- Yang, J. *et al.* *Ab initio* determination of the crystalline benzene lattice energy to sub-kilojoule/mole accuracy. *Science* **345**, 640–643 (2014).
- Hozoi, L. *et al.* Longer-range lattice anisotropy strongly competing with spin-orbit interactions in pyrochlore iridates. *Phys. Rev. B* **89**, 115111 (2014).
- Bogdanov, N. A. *et al.* Magnetic state of pyrochlore $\text{Cd}_2\text{Os}_2\text{O}_7$ emerging from strong competition of ligand distortions and longer-range crystalline anisotropy. *Phys. Rev. Lett.* **110**, 127206 (2013).
- Werner, H. J., Knowles, P. J., Knizia, G., Manby, F. R. & Schütz, M. Molpro: a general-purpose quantum chemistry program package. *Wiley Rev. Comp. Mol. Sci.* **2**, 242–253 (2012).
- Peterson, K. A., Figgen, D., Dolg, M. & Stoll, H. Energy-consistent relativistic pseudopotentials and correlation consistent basis sets for the $4d$ elements Y–Pd. *J. Chem. Phys.* **126**, 124101 (2007).
- Figgen, D., Peterson, K. A., Dolg, M. & Stoll, H. Energy-consistent pseudopotentials and correlation consistent basis sets for the $5d$ elements Hf–Pt. *J. Chem. Phys.* **130**, 164108 (2009).
- Dunning, T. H. Gaussian basis sets for use in correlated molecular calculations. I. The atoms boron through neon and hydrogen. *J. Chem. Phys.* **90**, 1007–1023 (1989).

40. Lim, I. S., Stoll, H. & Schwerdtfeger, P. Relativistic small-core energy-consistent pseudopotentials for the alkaline-earth elements from Ca to Ra. *J. Chem. Phys.* **124**, 034107 (2006).
41. Fuentealba, P., Preuss, H., Stoll, H. & von Szentpály, L. A proper account of core-polarization with pseudopotentials: single valence-electron alkali compounds. *Chem. Phys. Lett.* **89**, 418–422 (1982).
42. Fulde, P. Wavefunction-based electronic-structure calculations for solids. *Nat. Phys.* **12**, 106–107 (2016).
43. Fulde, P. *Correlated Electrons in Quantum Matter* (World Scientific, 2012).
44. Knowles, P. J. & Werner, H.-J. Internally contracted multiconfiguration-reference configuration interaction calculations for excited states. *Theor. Chim. Acta* **84**, 95–103 (1992).
45. Werner, H.-J. & Knowles, P. J. An efficient internally contracted multiconfiguration-reference configuration interaction method. *J. Chem. Phys.* **89**, 5803–5814 (1988).
46. Berning, A., Schweizer, M., Werner, H.-J., Knowles, P. J. & Palmieri, P. Spin-orbit matrix elements for internally contracted multireference configuration interaction wavefunctions. *Mol. Phys.* **98**, 1823–1833 (2000).
47. Bolvin, H. An alternative approach to the g -matrix: Theory and applications. *ChemPhysChem* **7**, 1575–1589 (2006).
48. Vancoillie, S., Malmqvist, P. & Pierloot, K. Calculation of EPR g tensors for transition-metal complexes based on multiconfigurational perturbation theory (CASPT2). *ChemPhysChem* **8**, 1803–1815 (2007).



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