

## Jahn-Teller Effect in Systems with Strong On-Site Spin-Orbit Coupling

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When strong spin-orbit coupling removes orbital degeneracy, it would at the same time appear to render the Jahn-Teller mechanism ineffective. We discuss such a situation, the  $t_{2g}$  manifold of iridates, and show that, while the Jahn-Teller effect does indeed not affect the  $j_{\text{eff}} = 1/2$  antiferromagnetically ordered ground state, it leads to distinctive signatures in the  $j_{\text{eff}} = 3/2$  spin-orbit exciton. It allows for a hopping of the spin-orbit exciton between the nearest-neighbor sites without producing defects in the  $j_{\text{eff}} = 1/2$  antiferromagnet. This arises because the lattice-driven Jahn-Teller mechanism only couples to the orbital degree of freedom but is not sensitive to the phase of the wave function that defines isospin  $j_z$ . This contrasts sharply with purely electronic propagation, which conserves isospin, and the presence of Jahn-Teller coupling can explain some of the peculiar features of measured resonant inelastic x-ray scattering spectra of  $\text{Sr}_2\text{IrO}_4$ .

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**Introduction.**—The discovery that spin-orbit coupling (SOC) can induce bulk insulators with conducting edge states, which are symmetry protected against backscattering, has in recent years revived interest in spin-orbit coupled materials [1,2]. While typical topological insulators are at most weakly correlated, the interplay of electron-electron interaction and spin-orbit coupling has also received enhanced attention. On one hand, the combination was soon discovered as a promising route to alternative topologically nontrivial states, from topological Mott [3,4] over fractional Chern [5] insulators to a potential realization [6,7] for Kitaev's celebrated spin-liquid phase with its anyonic excitations [8,9]. On the other hand, spin-orbit coupled and correlated square-lattice iridates are emerging as a sister system to high- $T_C$  cuprates [10–17].

The cupratelike physics and the Kitaev-Heisenberg model supporting the spin liquid are both understood to arise as the low-energy limit in iridium compounds like square-lattice  $\text{Sr}_2\text{IrO}_4$  [6,10,11] and honeycomb-lattice  $\text{Na}_2\text{IrO}_3$  [7,18]. In such iridates, the  $t_{2g}$  levels of the  $5d$  shell are almost filled, the single hole is subject to both strong SOC and appreciable correlations. The  $t_{2g}$  manifold can be described as an effective angular momentum  $l_{\text{eff}} = 1$ , and SOC locally couples spin  $\mathbf{s}$  and  $\mathbf{l}$  to a total angular momentum  $\mathbf{j}$ . The threefold orbital degeneracy of the  $t_{2g}$  states is thus lifted by SOC, and on-site Hubbard interaction can subsequently open a charge gap and stabilize a localized (pseudo)spin  $j_{\text{eff}} = 1/2$  [6,10]. Because of the orbital part of the  $j_{\text{eff}} = 1/2$  wave function,

couplings between these effective spins are sensitive to lattice geometry and support a variety of quantum states.

A striking difference to  $3d$  systems with negligible [19] SOC is the lifting of the orbital degeneracy: a single hole (or electron) in a  $3d$  shell has an orbital degree of freedom in addition to spin—as opposed to the single  $j_{\text{eff}} = 1/2$  degree of freedom of the  $5d$  hole. As a consequence, an analogous  $3d$  system can not only feature orbital order in addition to magnetism, but the Jahn-Teller effect [cf. Fig. 1(a)] would, moreover, be expected to couple the orbital degree of freedom to the lattice [20–23]. In contrast, the quenching of the orbital degree of freedom by SOC removes the possibility of orbital order and would at first sight also appear to suppress the Jahn-Teller effect and coupling to the lattice.

In this Letter, we are nevertheless going to discuss the impact of the Jahn-Teller effect on  $5d$  systems with strong SOC: While it is indeed absent for the ground state consisting of  $j_{\text{eff}} = 1/2$  pseudospins, see Fig. 1(b), we are going to show that it leaves clear signatures in the dynamics of collective *excitations* into the  $j_{\text{eff}} = 3/2$  sector (i.e., excitons). As seen in Fig. 1(c), the Jahn-Teller effect is here not quenched and can allow for a novel type of excitonic propagation. In particular, we propose that the experimentally observed branch of the exciton dispersion with the minimum at the  $\Gamma$  point [14], which cannot be explained using superexchange alone, finds a natural explanation within the present Jahn-Teller model.

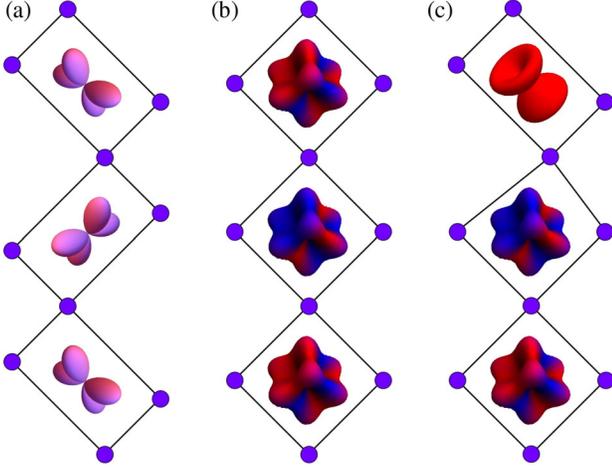


FIG. 1. Illustration showing the Jahn-Teller effect in systems *without* and *with* strong SOC. (a) Weak SOC—oxygen displacements following “conventional” Jahn-Teller effect for the ground state with, e.g., the  $d_{xz}/d_{yz}$  alternating orbital order. (b) Strong SOC—no oxygen displacements due to the quenched Jahn-Teller effect for the ground state with, e.g.,  $|j_{\text{eff}} = 1/2, j_z = 1/2\rangle/|j_{\text{eff}} = 1/2, j_z = -1/2\rangle$  alternating spin-orbital order (antiferromagnetic order of  $j_{\text{eff}} = 1/2$  isospins). (c) Strong SOC—oxygen displacements around the  $|j_{\text{eff}} = 3/2, j_z = -3/2\rangle$  exciton (which “lives” in the antiferromagnetic  $j_{\text{eff}} = 1/2$  ground state) showing that such a system is Jahn-Teller active.

*Finite Jahn-Teller for excited states.*—Since the SOC constant  $\lambda > 0$  is assumed to be the largest energy scale involved, with  $\lambda = 0.382$  eV in  $\text{Sr}_2\text{IrO}_4$  [14], we start our analysis by diagonalizing this dominant term. This is achieved by a basis change from  $\mathbf{s}$  (the  $s = 1/2$  spin) and  $\mathbf{l}$  (the effective  $l_{\text{eff}} = 1$  orbital moment) to total angular momentum  $\mathbf{j} = \mathbf{l} + \mathbf{s}$ . For a single hole in the  $t_{2g}$  shell, SOC interaction  $\mathcal{H}_{\text{SOC}} = \lambda \sum_i \mathbf{l}_i \cdot \mathbf{s}_i$  becomes then  $\mathcal{H}_{\text{SOC}} = \lambda/2 \sum_i (\mathbf{j}_i^2 - \mathbf{s}_i^2 - \mathbf{l}_i^2)$  and the ground state is given by the doubly degenerate  $j_{\text{eff}} = 1/2$  manifold, while the  $j_{\text{eff}} = 3/2$  manifold forms the excited states at energy  $3\lambda/2$ . (A crystal-field splitting  $\Delta$  can explicitly be included in this analysis [6,24], but is omitted here for clarity.)

For  $t_{2g}$  electrons, the orbital operators  $\mathbf{l}$  couple both to the tetragonal phonon modes  $Q_2$  and  $Q_3$  (the  $e_g$  modes) and to trigonal phonon modes  $Q_4$ ,  $Q_5$ , and  $Q_6$  (the  $t_{2g}$  modes). After integrating out the phonons, the Jahn-Teller interaction is expressed in terms of  $\mathbf{l}$  [21]:

$$\begin{aligned} \mathcal{H}_{\text{JT}} = & V \sum_{\langle i,j \rangle} \left[ (l_i^z)^2 - \frac{2}{3} \right] \left[ (l_j^z)^2 - \frac{2}{3} \right] \\ & + V \sum_{\langle i,j \rangle} [(l_i^x)^2 - (l_i^y)^2][(l_j^x)^2 - (l_j^y)^2] \\ & + \kappa V \sum_{\langle i,j \rangle} [(l_i^x l_i^y + l_i^y l_i^x)(l_j^x l_j^y + l_j^y l_j^x) + \dots]. \quad (1) \end{aligned}$$

The two classes of phonon modes lead to two *a priori* independent Jahn-Teller coupling constants  $V_{e_g} \equiv V$  and

$V_{t_{2g}} \equiv \kappa V$ ; as  $V_{t_{2g}}$  is typically much smaller than  $V_{e_g}$ , we set  $\kappa = 0.1$ . The Jahn-Teller interaction scale  $V$  can from experiment [25] be inferred to be non-negligible, but as its strength is at present unclear, we leave it as a free parameter.

The Jahn-Teller term  $H_{\text{JT}}$  is now, via straightforward but tedious calculations, transformed into the eigenbasis of  $\mathcal{H}_{\text{SOC}}$ , i.e., written in terms of  $j$  states:

$$\mathcal{H}_{\text{JT}} = \mathcal{H}_{\text{JT}}(1/2, 1/2) + \mathcal{H}_{\text{JT}}(3/2, 1/2) + \mathcal{H}_{\text{JT}}(3/2, 3/2). \quad (2)$$

The first term,  $\mathcal{H}_{\text{JT}}(1/2, 1/2)$ , denotes the Jahn-Teller interaction between two  $j_{\text{eff}} = 1/2$  states—it vanishes as expected, reflecting the quenching of orbital physics within the  $j_{\text{eff}} = 1/2$  subshell. The last term,  $\mathcal{H}_{\text{JT}}(3/2, 3/2)$ , between two  $j_{\text{eff}} = 3/2$  states can only contribute if a large number of  $j_{\text{eff}} = 3/2$  states are present and is thus strongly suppressed at large  $\lambda$ . The term  $\mathcal{H}_{\text{JT}}(3/2, 1/2)$  describes the interaction between one  $j_{\text{eff}} = 1/2$  and one  $j_{\text{eff}} = 3/2$  site: Even at strong SOC, this term becomes relevant when an (iso-)orbital excitation raises a single hole into a  $j_{\text{eff}} = 3/2$  state [13,14].

*Model.*—The  $j_{\text{eff}} = 3/2$  excitation, an exciton, can be created in resonant inelastic x-ray scattering (RIXS) and has been discussed in two recent theoretical and experimental studies [13,14]. It is described by the Green function

$$G(\mathbf{k}, \omega) = \text{Tr} \langle 0 | \hat{\chi}_{\mathbf{k}} \frac{1}{\omega - H + i\delta} \hat{\chi}_{\mathbf{k}}^\dagger | 0 \rangle, \quad (3)$$

where  $\hat{\chi}_{\mathbf{k}}^\dagger$  is a vector of four creation operators that create an exciton with momentum  $\mathbf{k}$  and isospin quantum number  $j_z = \pm 1/2, \pm 3/2$ . The Hamiltonian  $H$  describes the dynamics of the exciton coupling to a background of  $j_{\text{eff}} = 1/2$  isospins; a minimal Hamiltonian is

$$H = H_{\text{SE}}^{\text{mag}} + H_{\text{SE}}^{\text{exc}} + H_{\text{JT}}^{\text{exc}}. \quad (4)$$

The first term,  $H_{\text{SE}}^{\text{mag}}$ , is the superexchange interaction between  $j_{\text{eff}} = 1/2$  isospins, where we include up to third-neighbor processes  $\propto \{J_1, J_2, J_3\}$  [see Eq. (6) of the Supplemental Material of Ref. [14]]. It stabilizes an alternating order of  $j_{\text{eff}} = 1/2$  isospins with magnonlike excitations [13,14]. The terms  $H_{\text{SE}}^{\text{exc}}$  and  $H_{\text{JT}}^{\text{exc}} = \mathcal{H}_{\text{JT}}(3/2, 1/2)$  describe superexchange and Jahn-Teller interaction between one  $j_{\text{eff}} = 1/2$  and one  $j_{\text{eff}} = 3/2$  site; these terms allow the exciton to move.

Without the Jahn-Teller-mediated motion, i.e., for  $H = H_{\text{SE}}^{\text{mag}} + H_{\text{SE}}^{\text{exc}}$ , the problem was discussed in Refs. [13,14]. Exciton propagation due to superexchange is analogous to the mechanism governing orbital excitations in cuprates [26,27] and is strongly coupled to the magnonlike  $j_{\text{eff}} = 1/2$  excitations. We are going to show

here that the Jahn-Teller coupling  $\mathcal{H}_{JT}(3/2, 1/2)$  provides an additional channel for delocalization whose signatures can be clearly distinguished from the pure superexchange scenario.

Following Refs. [13,14], we extend a scheme that was widely used to describe motion in an antiferromagnetic background [28–31] in order to include Jahn-Teller-mediated exciton motion. The scheme amounts to applying Holstein-Primakoff, Fourier and Bogoliubov transformations (see Ref. [32] for details) to arrive at the Hamiltonian

$$H_{SE}^{\text{mag}} = \sum_{\mathbf{k}} \omega_{\mathbf{k}} a_{\mathbf{k}}^{\dagger} a_{\mathbf{k}}, \quad (5)$$

$$H_{SE}^{\text{exc}} + H_{JT}^{\text{exc}} = \sum_{\mathbf{k}} (\hat{E}_{\mathbf{k}}^{\text{SE}} + \hat{E}_{\mathbf{k}}^{\text{JT}}) \hat{\chi}_{\mathbf{k}}^{\dagger} \hat{\chi}_{\mathbf{k}} \quad (6)$$

$$+ \sum_{\mathbf{k}, \mathbf{q}} [(\hat{M}_{\mathbf{k}, \mathbf{q}}^{\text{SE}} + \hat{M}_{\mathbf{k}, \mathbf{q}}^{\text{JT}}) \hat{\chi}_{\mathbf{k}}^{\dagger} \hat{\chi}_{\mathbf{k}-\mathbf{q}} a_{\mathbf{q}} + \text{H.c.}]. \quad (7)$$

Equation (5) describes the isospin “magnons” originating from  $H_{SE}^{\text{mag}}$ ,  $a_{\mathbf{k}}^{\dagger}$  creates a magnon with momentum  $\mathbf{k}$  and energy  $\omega_{\mathbf{k}}$ ; see Ref. [32]. A free-exciton hopping is included in Eq. (6); it can either be due to second- and third-neighbor superexchange [14] or originate from coupling to the lattice. Finally, Eq. (7) captures the coupling between exciton hopping and the isospin background: Both the Jahn-Teller effect and superexchange can allow the exciton to exchange place with a nearest-neighbor isospin without flipping said isospin. This creates “faults” in the alternating order, see Fig. 4(a), and thus creates or annihilates magnons.

Let us now discuss in more detail the contributions due to the Jahn-Teller effect; for the pure superexchange problem, we refer to Refs. [13,14]. The Jahn-Teller vertex  $\hat{M}_{\mathbf{k}, \mathbf{q}}^{\text{JT}}$  and the free-excitonic dispersion  $\hat{E}_{\mathbf{k}}^{\text{JT}}$  are calculated here from  $\mathcal{H}_{JT}(3/2, 1/2)$  and read  $\hat{M}_{\mathbf{k}, \mathbf{q}}^{\text{JT}} = zV\hat{m}^{\text{JT}}|\gamma_{\mathbf{k}}v_{\mathbf{q}} + \gamma_{\mathbf{k}-\mathbf{q}}u_{\mathbf{q}}|/\sqrt{N}$  and  $\hat{E}_{\mathbf{k}}^{\text{JT}} = zV\hat{e}^{\text{JT}}|\gamma_{\mathbf{k}}|$ , where  $N$  is the total number of sites,  $z = 4$  is the coordination number for a square lattice, and  $\gamma_{\mathbf{k}} = \frac{1}{2}(\cos k_x + \cos k_y)$ . The Bogoliubov coefficients  $u_{\mathbf{k}}, v_{\mathbf{k}}$  and the diagonal (off-diagonal) matrix  $\hat{m}^{\text{JT}} (\hat{e}^{\text{JT}})$  are explicitly given in Ref. [32]. The crucial new feature will turn out to come from the free dispersion  $\hat{E}_{\mathbf{k}}^{\text{JT}}$ , where the Jahn-Teller effect induces a nearest-neighbor contribution absent from superexchange.

**Results.**—We evaluate the Green function Eq. (3) using the self-consistent Born approximation (SCBA)—a diagrammatic approach that takes into account diagrams of rainbow type (see, e.g., Ref. [28]). The excitonic spectral functions are calculated numerically for a  $32 \times 32$  cluster, taking into account “matrix elements” depending on the angle of the incident beam [14], and shown in Fig. 2. The most striking difference from the pure superexchange scenario becomes visible in the so-called “normal” RIXS geometry [cf. Fig. 2(a)]: a dispersive feature at around

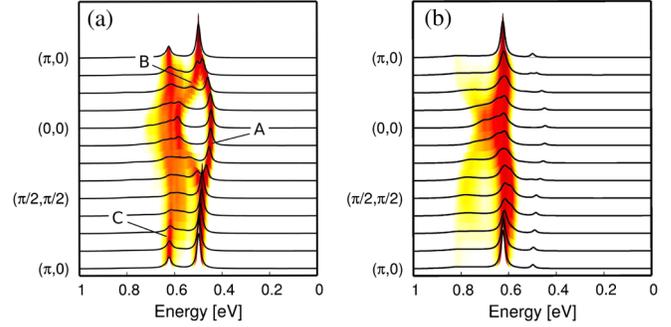


FIG. 2. Spin-orbit exciton with both superexchange and Jahn-Teller interaction, see Eqs. (5)–(7), calculated using the SCBA. Intensities are given for two RIXS geometries: (a) normal and (b) grazing incidence [14]. A, B, C in (a) denote three main features of the spectrum. Jahn-Teller interaction  $V = 0.8J_1$  and broadening  $\delta = 0.05J_1$ . Superexchange parameters  $J_2 = -0.33J_1$ ,  $J_3 = 0.25J_1$ ,  $W_1 = 0.5J_1$  [14], and  $W_2 = W_3 = 0$ . Following Ref. [14], on-site energy of the exciton is  $10J_1 \approx \frac{3}{2}\lambda$ , crystal-field splitting between  $|j_z| = 1/2$  and  $|j_z| = 3/2$  states is  $2.29J_1$ , and  $J_1 = 0.06$  eV.

0.4 eV (denoted as A in the figure) that has its minimal energy at  $\mathbf{k} = (0, 0)$  and disperses upward towards the zone boundary, where it merges with the B feature.

An unexplained feature with minimum at the  $\Gamma$  point was observed in normal-incidence RIXS experiments on  $\text{Sr}_2\text{IrO}_4$  [14], albeit with a weaker intensity. This discrepancy may be due to (i) contributions to the RIXS intensity of the exciton beyond the one determined in the fast core-hole approximation [34,35] or (ii) the SCBA overemphasizing the quasiparticle spectral weight [14]. Some fine-tuning of the unknown constant  $V$  is needed to reproduce the experimental dispersion, especially the merging with the B feature; see Ref. [32] for details. It is worth noting here that a similar peak was also seen in  $\text{Na}_2\text{IrO}_3$  [36], where it does not merge with the higher-energy features, suggesting that the merging may be a detail specific to  $\text{Sr}_2\text{IrO}_4$ . In contrast and as discussed below, the minimum at the  $\Gamma$  point is a robust and characteristic feature of Jahn-Teller-mediated propagation, because superexchange-driven peaks invariably have a *maximum* at the  $\Gamma$  point.

**Discussion.**—Figure 3 illustrates the qualitative difference between Jahn-Teller- and superexchange-mediated exciton propagation, with Figs. 3(a) and 3(c) showing the purely Jahn-Teller ( $H_{SE}^{\text{exc}} \equiv 0$ ) and purely superexchange ( $H_{JT}^{\text{exc}} \equiv 0$ ) scenarios. A striking difference is that the two quasiparticlelike branches of the superexchange case [Fig. 3(c)] become four in the Jahn-Teller case [Fig. 3(a)]—one of which indeed has a minimum at the  $\Gamma$  point. We continue the analysis by noting that both mechanisms allow in principle for a “free” dispersion without disturbing the alternating isospin order, see Eq. (6), as well as for a “polaronic” propagation involving magnons, see Eq. (7). Figures 3(b) and 3(d) include only the latter and reveal that the two mechanisms are then

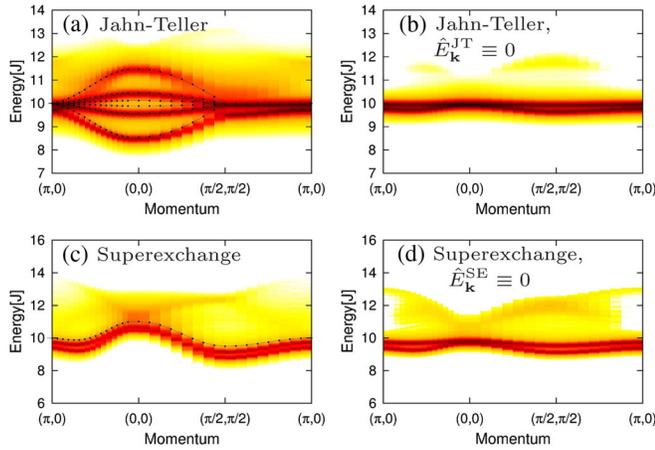


FIG. 3. Spin-orbit exciton spectra with propagation driven by either superexchange *or* Jahn-Teller interaction (calculated using SCBA, see text): (a) Jahn-Teller only, (b) Jahn-Teller only *and* setting  $\hat{E}_k^{\text{JT}} \equiv 0$ , (c) superexchange only, (d) superexchange only *and* setting  $\hat{E}_k^{\text{SE}} \equiv 0$ . For clarity, parameters are chosen slightly different from those used in Fig. 2:  $J_2 = -0.33J_1$ ,  $J_3 = 0.25J_1$ ,  $W_1 = 0.5J_1$ ,  $W_2 = W_3 = 0.13J_1$  [14], Jahn-Teller interaction  $V = J_1$  and broadening  $\delta = 0.05J_1$ . Spectra are offset by the exciton energy of  $10J_1 \approx \frac{3}{2}\lambda$ . Dotted lines in (a) and (c) follow the free-dispersion relations given by  $\hat{E}_k^{\text{JT}}$  and  $\hat{E}_k^{\text{SE}}$ , respectively.

almost indistinguishable. This points to a dominant role for isospin fluctuations (on the scale of  $J$  in both scenarios) in the polaronic part of exciton motion.

This brings us to the following question: Is the difference between the free-dispersion relation in the superexchange and in the Jahn-Teller generic, or is it just a matter of fine-tuning of the parameters? It turns out that the difference between these two dispersion relations is of fundamental nature. The crucial aspect concerns the nearest-neighbor process, which is therefore depicted for superexchange and Jahn-Teller effect in Fig. 4. In superexchange, the exciton propagates by exchanging place with an isospin while both conserve their “spin,” i.e., their  $j_z$  quantum number. In an alternating isospin order, where nearest neighbors are always of opposite  $j_z$ , this necessarily creates or removes “defects,” see Fig. 4(a), and thus magnons. The Jahn-Teller effect, in contrast, allows the exciton and the isospin to flip their quantum numbers while exchanging places, and this allows for the nearest-neighbor hopping of an exciton without creating magnons, i.e., a free-excitonic dispersion, see Fig. 4(b). The origin of the difference is that the hole hopping driving superexchange conserves the  $j_z$  quantum number, while the lattice-mediated Jahn-Teller effect is insensitive to the orbital phase. This allows  $j_z$  to change during Jahn-Teller-driven propagation and accordingly yields four quasiparticles rather than two.

*Conclusions.*—We analyzed here the impact of a lattice-mediated Jahn-Teller effect in the presence of strong SOC, which quenches orbital degeneracy in the ground state. We found that the Jahn-Teller effect remains present for excited

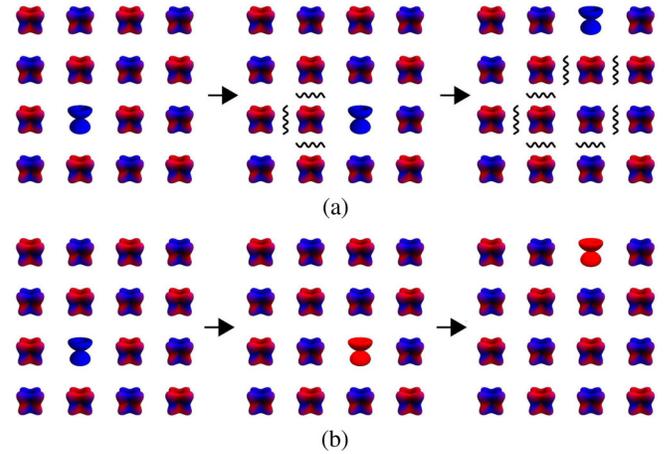


FIG. 4. Illustration showing the two types of nearest-neighbor hopping of a  $j_{\text{eff}} = 3/2$  exciton in the antiferromagnetically ordered background. (a) Polaronic hopping (due to Jahn-Teller effect *or* superexchange): a  $j_{\text{eff}} = 3/2$  exciton with the  $j_z = -3/2$  quantum number (left-hand panel) does not change its  $j_z$  quantum number during the hopping process to the nearest-neighbor sites (middle and right-hand panels) and thus the  $j_{\text{eff}} = 1/2$  magnons are created at each step of the excitonic hopping (wiggly lines on middle and right-hand panels). (b) Free hopping (solely due to Jahn-Teller effect): a  $j_{\text{eff}} = 3/2$  exciton with the  $j_z = -3/2$  quantum number (left-hand panel) hops to the nearest-neighbor site and acquires  $j_z = 3/2$  quantum number (middle panel). Note that in this case the  $j_{\text{eff}} = 1/2$  magnons are *not* created in the system (middle and right-hand panels).

states, and, in particular, allows for a free nearest-neighbor hopping of the spin-orbit exciton without producing defects in the alternating  $j_{\text{eff}} = 1/2$  ordering of the ground state. The telltale spectral signature is a dispersion with a minimum at the  $\Gamma$  point, which was observed in experiment but cannot be explained with superexchange alone [14]. Experiments on  $\text{Sr}_2\text{IrO}_4$  at higher temperatures moreover reveal an active orbital degree of freedom and its coupling to the lattice [25], corroborating the relevance of Jahn-Teller physics when going beyond the ground state.

We have found spin-orbit coupling to substantially affect the interplay of Jahn-Teller effect and superexchange. In  $3d$  compounds with weak spin-orbit coupling and unquenched orbital degeneracy (e.g., in manganites [37,38]), both act on the same microscopic degree of freedom (i.e., orbitals) and in general lead to similar signatures. In the strongly spin-orbit-coupled  $5d$  case, however, Jahn-Teller effect (determined purely by the orbital) and superexchange (strongly affected by spin-orbit entanglement) address different microscopic degrees of freedom. Their interplay is thus far more intricate, as is coupling between ions with and without strong spin-orbit coupling [39].

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